# ACCURACY OF ATLANTIC TROPICAL CYCLONE FORECASTS

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#### **ABSTRACT**

During the past several years a number of techniques have been developed for forecasting the motion of tropical cyclones over areas of the Atlantic, Caribbean, and Gulf of Mexico. Many of these have been tested on an operational basis. These forecasts have been collected and verified and probability ellipses have been constructed. While direct comparisons between the forecast methods are difficult (because of inhomogeneity of sample size, differences in times of availability of the forecasts, etc.), it has been found that two of the objective techniques tested result in slightly better forecasts than the others. The accuracy of the forecasts depends somewhat on the geographical area and the forecast error varies almost linearly with the length of the forecast period.

#### 1. INTRODUCTION

A continuing and developing program for the evaluation of the performance of the various techniques utilized in predicting the future course of hurricanes has been in existence at the National Hurricane Center (NHC), Miami, Fla., for several years. Sufficient data have now been accumulated to permit meaningful conclusions to be drawn as to the relative merits of some of the numerous systems which have been used to forecast hurricane motion. In this paper, attention will be focused on the performance of eight such techniques during the years 1959-64, although not all methods were used throughout the entire period. The first part deals with a number of statistical measures of the forecast errors. The second part presents verification information in the form of probability ellipses for four levels of probability, namely, 20, 40, 60, and 80 percent.

It is not the purpose of this paper to discuss in detail the forecast techniques which have been evaluated, since most of these have been described elsewhere [4, 5, 8, 9, 10]. However, in order to facilitate reading of the paper a brief summary of the main features of each method will be given. The methods range from simple straight-line extrapolation to numerical prediction with a simple barotropic model. Several are statistical in nature and were derived by a screening and multiple linear regression technique. As predictors, these use such parameters as sea level pressures or heights of constant pressure surfaces, geostrophic wind components, the past motion of the cyclone center, thicknesses between constant pressure surfaces, and height changes measured in a moving coordinate system. The official forecasts issued by the Weather Bureau Forecast Centers represent the professional judgment and experience of the hurricane forecasters, and are essentially subjective in nature, although consideration is given to the numerical forecasts, objective aids, climatology, etc. The basic characteristics of each method are listed in table 1.

In verifying the forecasts a "best track" prepared by the Hurricane Forecast Centers was used, the writer having no part in determining this track. With one exception, only those forecasts prepared at the time of the event for operational forecast purposes were verified. In an earlier paper the writer [7] described a set of "simulated" operational forecasts prepared by use of the T-60 method. The verification statistics for this method in-

Table 1.—Forecast methods which were verified. Symbols in column 2 have the following meaning:

Pz, Py Past motion of the cyclone center Sea level pressure

P H, Z, u, v

700-mb. height 500-mb. height geostrophic wind component

 $\Delta Z_{10/7}$  1000-700-mb. thickness  $\Delta Z_{7/5}$  700-500-mb. thickness 700-500-mb. thickness 700-mb. height change δZ<sub>5</sub>/δt 500-mb. height change

Method	Predictors used	Forecast periods
Official Weather Bureau Advisory (WB)  Numerical Weather Prediction (NWP)  Travelers Synoptic Climatological 1959 (T-59)  Travelers-National Hurricane Research Laboratory-1960 (T-60)  National Hurricane Center-1964 (NHC-64)  Riehl-Haggard-Sanborn (RHS)  Miller-Moore (MM)  Persistence (PERS)	climatology. Barotropic model (500 mb.) $P, P_s, P_y$ $P_s, P_s, P_y$ $P_s, P_s, P_s, P_s, P_s, P_s, P_s, P_s, $	12, 24, 48, 72 hr. 12 to 72 hr. by 12-hr. steps. 24 hr. 24 and 36 hr. 12 to 48 hr. by 12-hr. steps. 24 hr. 24 hr. 12 to 72 hr. by 12-hr. steps.

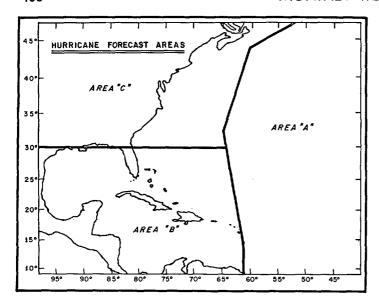


FIGURE 1.—Hurricane forecast areas.

clude the simulated forecasts for the years 1959-60 in addition to those prepared for the other years. Most of the statistical measures were obtained by computer methods, which virtually eliminated the possibility for computational errors.

Previous studies by Gentry [3], Dunn [2], and Tracy [7] have indicated that the accuracy of hurricane forecasts varies from one geographical area to another. For this reason the verification statistics have been stratified according to area (fig. 1). Area B has the largest number of oceanic upper-air stations and area A has the fewest.

Differences in the verification statistics have been attributed to the differences in the data density, although other factors (such as climatology) may contribute to these differences.

Before a detailed examination of the statistical quantities, some comments and a word of caution are in order concerning the interpretation of these results. While comparisons as to the relative merits of the techniques are inevitable, these comparisons may not be fully justified. The sample sizes are unequal, and not all methods were used during all the years. For example, NHC-64 was used for the first time during the 1964 season, but routine preparation of the RHS and T-60 forecasts was discontinued at Miami in 1964. This made it impossible to obtain a homogeneous sample for comparison of all techniques, although a small homogeneous sample was available for comparing five forecast methods based on the 1964 season. In addition, the official Weather Bureau forecasts are issued at 6-hour intervals, beginning at 0400 GMT. This means that the 24-hr. forecasts issued at 0400 GMT and 1600 GMT are based on surface and upper-air data observed 4 hours earlier, while those issued at 1000 GMT and 2200 GMT are based on upper-air data observed 10 hours earlier. On the other hand, the forecast period for the objective systems is measured from observation time, even though the forecast may not be available until several hours later. This places the official forecasts at a disadvantage whenever comparisons between methods are made, but this disadvantage is partly offset by the availability of later data, particularly aircraft reconnaissance reports.

Table 2.—Statistical data for 24-hr. forecast period, 1959 through 1964.

Name of technique	1	NHC-64	<b>!*</b>		NWP	;		. <b>T</b> –59			М-М			T-60#			RHS		, ,	PERS	
Area Number of	A	В	C .	A	В	C	A	В	С	A	В	C	A	В	C	A	? <b>B</b>	С	A	В	С
forecasts	7	46 88	15	75	126	52	114	254	127	8	103	38	102	284	51	11	111	29	280	414	199
Mean (n. mi.) Standard de- viation (n.	98	. 88	156	190	133	159	147	116	164	155	96	140	150	112	168	251	130	145	235	134	206
mi.)	44	51	. 86	155	85	98	106	66	92	69	57	82	126	67	97	120	84	100	192	86	121
Median (n.				1						1						1	-				
_ mi.)	102	83	. 142	153	114	139	126	106	143	.177	87	117	114	97	169	266	120	108	175	115	179
(n. mi.) Upper quartile	48	47	95	96	80	80	78	67	91	91	54	75	75	64	77	147	73	76	101	73	116
(n. mi.)	48-189	116 13-245	173 34–370	244 13-949	179 13-614	213 26-496	177 13-747	158 0-430	230 6–401	215 26-228	125 6-271	167 25–343	180 21-793	151 8–365	229 25-377	297 79–545	164 13-544	165 12-401	317 16-1270	169 8-578	277 10-611

<sup>\*1964,</sup> only. #1959-1963.

Table 3.—Statistical data for 36-hr. Forecast Period, 1959 through 1964.

Name of technique	N	HC-64*		NWP			T-60#			PERS		
Area Number of forecasts Mean (n. mi.) Standard deviation (n. mi.) Median (n. mi.) Lower quartile (n. mi.) Upper quartile (n. mi.) Range (n. mi.)	A 7 186 83 176 123 209 45–331	B 46 145 74 151 75 195 32-306	C 252 105 231 174 290 113-514	A 65 281 259 238 124 344 12–1445	B 121 210 158 183 114 256 30–1332	C 37 272 169 237 142 350 24-830	A 88 212 165 178 115 251 19–1177	221 195 124 181 98 253 0-755	C 44 231 125 245 107 327 21–496	A 117 309 253 234 134 408 6-1329	B 269 209 134 174 112 269 19–730	C 70 317 194 268 173 424 36–941

<sup>\*1964</sup> only.

Table 4.—Statistical data for 48-hr. forecast period

Name of technique		NHC-6	4*		NWP			PERS#			
Area Number of	A	В	C	A	В	C	A	В	c		
forecasts Mean (n. mi.) Standard	7 264	45 211	13 420	45 314	97 273	36 407	79 313	131 279	56 473		
deviation (n. mi.) Median	107	106	154	203	161	212	203	138	284		
(n. mi.) Lower quartile	288	197	407	283	247	405	254	254	<b>434</b>		
(n. mi.) Upper quartile	151	119	310	155	160	234	156	174	217		
(n. mi.) Range	302	288	435	440	345	529	429	351	686		
	68~430	35-408	212-747	51-786	43-902	75-1093	33-1100	37-633	78-1212		

<sup>\*1964</sup> only. †1959-64. #1962-64.

Table 5.—Statistical data for 72-hr. forecast period, 1964

Name of technique		NWP		PERS			
Area.  Number of forecasts Mean (n. mi.) Standard deviation (n. mi.) Median (n. mi.) Lower quartile (n. mi.) Upper quartile (n. mi.) Range (n. mi.)	A 10 467 218 528 248 651 54-698	B 24 423 244 346 235 608 71–925	C 525 306 556 83 684 83–906	A 49 436 293 377 181 608 0-1188	B 66 449 232 430 271 557 48–1086	C 12 752 375 812 353 1038 157–1285	

# 2. DISCUSSION OF RESULTS BY GEOGRAPHICAL AREAS

The results of the statistical analyses are shown in tables 2-8, with the verification numbers stratified by geographical areas (fig. 1). Table 2 presents the results of the error-record of the seven methods for a 24-hr. forecast period. One of the most striking facts brought out by this table is that for all systems the errors were for the most part substantially less in area B than in either areas A or C. The standard deviations were generally smaller in area B than in the other areas. This indicates that the errors in the distribution were more closely clustered about the mean. Observing the upper quartiles, one notes that there is quite a large reduction in the magnitudes of these errors in area B when compared with the other areas. This shows that there were considerably fewer large-error types of forecasts made in area B than in A or C. This same fact is noticed when most of the other statistical items in table 2 are examined.

The data in table 2 seem to indicate that the NHC-64 and M-M techniques produced 24-hr. forecasts with the smallest vector errors. For example, the mean and median vector errors for NHC-64 and M-M in area B are 88 and 83 n. mi. and 96 and 87 n. mi., respectively. These are substantially less than those of the other systems.

The 36-hr. forecast errors for the four systems which produce 36-hr. forecasts are shown in table 3. These data indicate that NHC-64 produced forecasts with the smallest

Table 6 .- Official Weather Bureau forecasts, 1959 through 1964

Forecast period	Area	Num- ber of fore- casts	Mean (n. mi.)	Stand- ard de- viation (n. mi.)	Me- dian (n. mi.)	Lower quar- tile (n. mi.)	Upper quar- tile (n. mi.)	Range (n. mi.)
24 hr	A	289	183	138	138	85	237	5-812
	B	406	113	71	96	60	152	6-395
	C	194	167	94	150	93	216	7-502
48 hr.*	A	104	271	164	243	140	346	8-787
48 hr	B	153	237	132	212	142	304	21-708
48 hr	C	57	381	218	344	189	519	33-880
72 hr.†	A	53	390	252	332	212	472	102-1236
72 hr	B	65	362	217	335	210	470	55-998
72 hr	C	10	403	164	410	254	448	130-670

<sup>\*</sup>Began in 1961. †Started in 1964.

Table 7.—Statistical data for 24-hr. forecast period. Homogeneous for 1964

Name of technique	Number of forecasts	Mean (n. mi)	Standard deviation (n. mi.)	Mean (n. mi.)	Lower quartile (n. mi.)	Upper quartile (n. mi.)	Range (n. mi.)
PERS	23 23 23 23 23 23	120 101 127 107 127	85 56 71 60 52	105 97 94 88 136	48 54 80 60 73	128 142 168 124 163	24-357 6-219 26-278 44-321 42-202

Table 8.—Forecast system having the least mean error by areas and forecast periods

Forecast period		24	hr.	_			36 hr.		
Area		64 N 7 98 02	B VHC-64 46 88 83	3 14	8	A HC-64 7 186 176		-64 46 145 151	C T-60 44 231 245
Forecast period		48	8 hr.				72 hr.		
Area. Method Number of forecasts Mean (n. mi.). Median (n. mi.).	2	64 N 7 164 188	B VHC-64 42 211 197	. 40	16	A PERS 49 436 377		WP 24 423 346	C NWP 4 525 556
	OFFIC	IAL '	WB F	RECA	STS				
Forecast period	2	4 hr.		4	18 br.			72 hr.	
Forecast period when referred to synoptic map time	2	8 hr.			52 hr.		7	76 hr.	
Area Number of forecasts Mean (n. mi.) Median (n. mi.)	A 289 183 138	B 406 113 96	C 194 167 150	A 104 271 243	B 153 237 212	C 57 381 344	A 53 390 332	B 65 362 335	403

vector errors in area B, where the mean was 145 n. mi. The T-60 was the next best with a mean error of 195 n. mi. In area C the mean error for T-60 was lower, but the median for NHC-64 was lower. However, the results of the two systems are not strictly comparable since they are for different years.

For a 48-hr. forecast three systems could be compared (table 4). The NHC-64 errors are less in A and B than

either the NWP or PERS errors, while in C the NWP has a better record.

For a 72-hr. forecast (table 5), the NWP is better than persistence in areas B and C, while persistence is better in A. This latter fact is supported by Colón's [1] finding that a persistence forecast in the area east of the Lesser Antilles has a high probability of success.

Table 6 presents the statistical items for the official Weather Bureau forecasts. These data are listed separately because of the differences in the times these forecasts are issued. While no direct comparisons between the WB forecasts and the various objective systems should be made, it is of interest to note that the two best objective systems (NHC-64 and M-M) have demonstrated forecast skill comparable to that of the official forecasts. Table 6 also shows that forecasts for area B are better than those in areas A or C.

Table 7 shows the result of a homogeneous comparison of forecasts obtained by five of the objective forecast systems during the hurricane season of 1964. Homogeneous comparison as used here indicates that a forecast was "simultaneously" obtained by each of the five methods employed for the same synoptic times for the hurricanes of 1964. It was only possible to obtain 23 cases meeting this criterion. The data in this table show that for these 23 cases the NHC-64 and M-M techniques demonstrated somewhat superior performance over the NWP, T-59, and PERS systems. This is evident from a comparison of the means and medians of the vector errors.

The results of this section may be summarized briefly. Most of the forecast systems verified produce better forecasts in area B than elsewhere. This is the area with the greatest density of oceanic upper-air stations, and part of the increased accuracy is probably due to the better analyses which can be produced with more data. However, if one examines the persistence forecasts one finds that they are also significantly better in area B for 24-, 36-, and 48-hr. forecasts. This probably indicates that some of the increased forecast accuracy in area B is due to climatological factors. Finally, a 6-year record for the Miller-Moore technique and a 1-year record for the NHC-64 method indicate that these two systems are capable of producing somewhat better forecasts than the other objective methods tested. This is shown by the homogeneous sample (table 7) as well as table 8, which lists the forecast system having the least mean error by areas and forecast periods.

## 3. CHANGE IN VECTOR ERRORS WITH TIME

Figures 2a, 2b, and 2c contain plots of the mean vector error as a function of the forecast period for three of the hurricane track forecasting techniques. The three methods that are plotted are the NHC-64, NWP, and WB. The data are for area B, and include 1959-1964 for WB and NWP, but 1964 only for NHC-64.

The figures show that for all three methods there is very

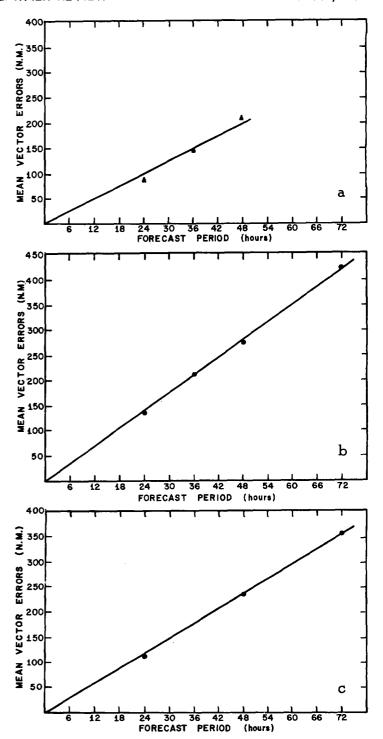


FIGURE 2.—Vector errors as a function of a change in the forecast period (a) NHC-64 method, (b) NWP method, (c) Weather Bureau official forecasts.

nearly a linear relationship between mean vector errors and length of forecast period.

# 4. PROBABILITY ELLIPSES

In this section the forecast vector errors will be displayed by use of probability ellipses. Figures 3 through 21 show probability ellipses for a number of techniques for 24-hr. forecast periods.

In the figures the origin (cross) represents the forecast position of the storm and the small dots represent the observed position of the storm at verification time relative to the forecast position. Thus, the error distribution represented by these figures may be interpreted in the following way:

Quadrant <sup>1</sup> 1—forecast position too far south and east. Quadrant 2—forecast position too far south and west. Quadrant 3—forecast position too far north and west. Quadrant 4—forecast position too far north and east. The numbers appearing on the probability ellipses represent the probabilities that that percentage of the distribution of the vector errors will be contained within these ellipses.

Before proceeding with a summary discussion of the figures, some comments regarding probability ellipses will be offered. Following Veigas, Miller, and Howe [9], the vector errors were resolved into latitude and longitude components and were plotted on suitable figures. Then, if it is assumed that these components, when considered jointly, may be displayed as a bivariate normal distribution (see Appendix), the resulting equations (1)-(3) from the probability density function are as follows:

$$a^{2} = \frac{2(1-\rho^{2}) \ln S}{\frac{1}{\sigma_{long}^{2} - \frac{\rho}{\sigma_{long}\sigma_{lat}}} \tan \phi}$$
(1)

$$b^{2} = \frac{2(1-\rho^{2}) \ln S}{\frac{1}{\sigma_{lat}^{2}} + \frac{\rho}{\sigma_{lons}\sigma_{lat}} \tan \phi}$$
 (2)

where a is the semi-major axis and b is the semi-minor axis of an ellipse. The other terms in equations (1) and (2) are defined as follows:  $\sigma_{long}$  and  $\sigma_{lat}$  are the population standard deviations of the longitude and latitude components, respectively;  $\rho$  is the linear correlation coefficient between the longitude and latitude components; and S is a measure of the probability and is given by S=1/(1-p) where p is a certain probability, e.g., 10 percent, 28 percent, etc.

$$\phi = \frac{1}{2} \arctan \frac{2\rho\sigma_{long}\sigma_{lat}}{\sigma_{long}^2 - \sigma_{lat}^2}$$
 (3)

where  $\phi$  is the angle which the semi-major axis of an ellipse makes with the horizontal coordinate axis of the figure depicting the error distribution. To solve the above equations, estimates of the various population parameters were obtained from the data sample represented in each figure.

Table 9 is a summary of some of the relationships

Table 9.—Summary of some of the relationships represented by the probability ellipses depicted in figures 3 through 21. 24-hr. forecast periods represented.

			A	ver	ige b	ias of asts	the	covere for a	ative ar ed by ell particu echnique	Probability contours ap- proximately		
Name of technique	Fig. No.	Area	Too far N			Too slow	None	Small- est	In be- tween	Larg- est	Cir- cular	Ellip- tical
WB WB WB WB WB WB WB M-M M-M M-M M-M T-59 T-59 T-59 T-59 T-59 T-59 T-60 T-60 T-60 PERS PERS PERS	3 4 5 6 7 8 9 10 111 122 13 144 15 166 177 18 19 20 21	ABCBCBCABCABCABC	XXXX	X X X X X	X X X X X X X	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	X	X X X X	X X X X	X X X X	X	X X X X X X X X X X X X X X X X X X X

represented by the probability ellipses depicted in figures 3 through 21. This table identifies the name of the forecast method being considered, the number of the figure which gives the detailed data for that forecasting technique, the area in which the data represented was acquired, a comparison of areas for each system depicted, and an observation of the degree to which the probability ellipses depart from ellipticity. Table 10 contains a section showing the percentage of forecasts which should be contained within the areas of the probability ellipses if the assumption is met that the joint distribution of the latitude and longitude components of the vector errors is a bivariate normal one, and the actual percentage of these forecasts which are contained within these probability ellipses. Also appearing in this table are the allowable differences in percentages permitted between a bivariate normal distribution and an actual distribution.

In conclusion, tables 9-10, illustrate several facts concerning figures 3 through 21.

First, for all techniques the forecasts made while storms were in area B yielded the smallest errors.

Second, most of the methods examined exhibited some sort of bias, even though it was quite small for some of the methods. For example, forecasts made while storms were in area A with the WB, T-59, NWP, and PERS methods produced forecasts which, on the average, tended to be too far south and too fast with reference to the observed positions of the storm centers.

Forecasts made when storms were in area B with the WB and RHS systems produced forecasts which, on the average, tended to be too far north and too fast, while those using the M-M and T-60 techniques produced "on the average" forecasts which tended to be too far north and too slow. Forecasts made in area B by the T-59 and NWP methods exhibited primarily a bias toward being too fast.

<sup>&</sup>lt;sup>1</sup> Quadrants are numbered by considering Quadrant 1 to be the upper lefthand quadrant, Quadrant 2 the upper righthand quadrant, Quadrant 3 the lower righthand quadrant, and Quadrant 4 the lower lefthand quadrant. These quadrants are with reference to the coordinate axes not with reference to the ellipses.

Table 10.—Percentage of forecasts contained within probability ellipses. Bivariate normal percentages (5 percent level)

			20% probab	oility ellipse	40% probab	oility ellipse	60% probab	ility ellipse	80%probab	ility ellipse
Name of technique	Figure No.	Area	Actual percentage	Maximum allowable absolute difference	Actual percentage	Maximum allowable absolute difference	Actual percentage	Maximum allowable absolute difference	Actual percentage	Maximum allowable absolute difference
			Percent	Percent	Percent	Percent	Percent	Percent	Percent	Percent
WB. WB. WB. M-M. M-M. R-H-S. R-H-S. T-59. T-59. NWP. NWP. NWP. NWP. T-60. T-60. T-60. T-60. T-60. T-61. T-62. PERS. PERS.	3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21	A B C B C B C A B C A B C A B C	34 26 21 22 18 27 28 27 21 22 22 21 39 22 22 29 36 25 21	8. 0 6. 7 9. 8 13. 4 22. 1 13. 1 24. 6 12. 8 15. 7 12. 1 18. 9 13. 5 8. 9 19. 0 9. 4 7. 6 11. 1	55 46 43 41 45 47 59 51 40 46 48 59 44 41 59 46 47	8. 0 6. 7 9. 8 13. 4 22. 1 13. 1 24. 6 12. 8 5. 4 12. 1 15. 7 12. 1 18. 9 13. 5 8. 9 19. 0 9. 4 7. 6	69 62 59 61 71 72 70 56 61 67 67 63 55 71 67	8. 0 6. 7 9. 8 13. 4 22. 1 13. 1 24. 6 12. 8 5. 4 12. 1 15. 7 12. 1 18. 9 13. 5 8. 9 19. 0 9. 4 7. 6 11. 1	83 77 77 73 76 88 79 85 76 72 79 79 73 84 78 69 83 79	8.0 6.7 9.8 13.4 22.1 124.6 12.8 15.7 12.1 18.7 13.5 8.9 19.0 9.4 7.6

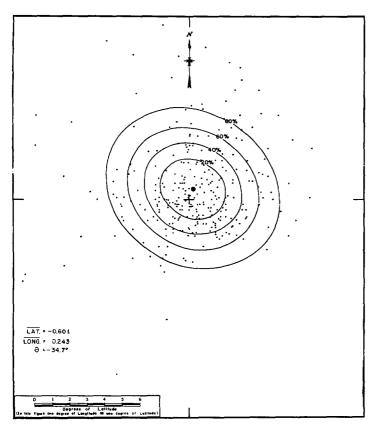


Figure 3.—Probability ellipses for Weather Bureau 24-hr. forecasts, area A (1959-64). Numbers in lower left are as follows: LAT.—average of latitude component (in °lat.); LONG.—average of longitude component (in °lat.); θ—angle formed by semi-major axis with the horizontal axis of the figure. Bold dot indicates center of ellipses; cross indicates origin of coordinate axes.

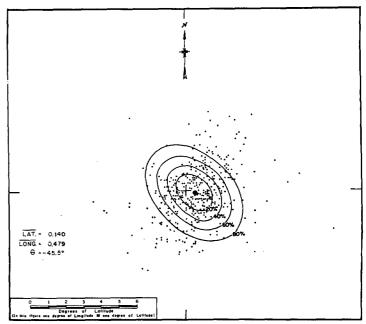


FIGURE 4.—Probability ellipses for Weather Bureau 24-hr. forecasts, area B (1959-64). For explanation see figure 3.

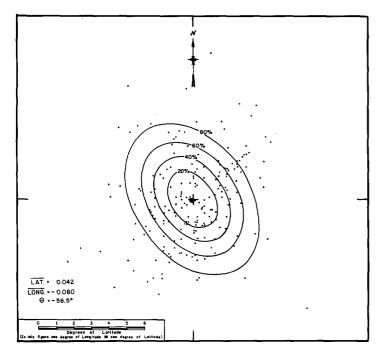


Figure 5.—Probability ellipses for Weather Bureau 24-hr. forecasts, area C (1959-64). For explanation see figure 3.

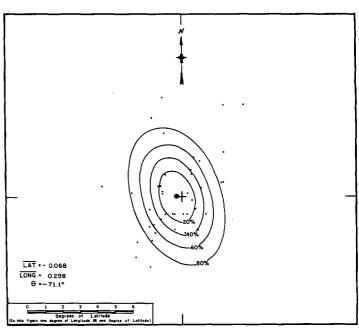


Figure 7.—Probability ellipses for modified Miller-Moore method, area C (1959-64). For explanation see figure 3.

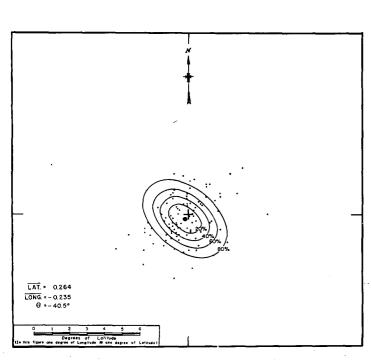


FIGURE 6.—Probability ellipses for modified Miller-Moore method, area B (1959-64). For explanation see figure 3.

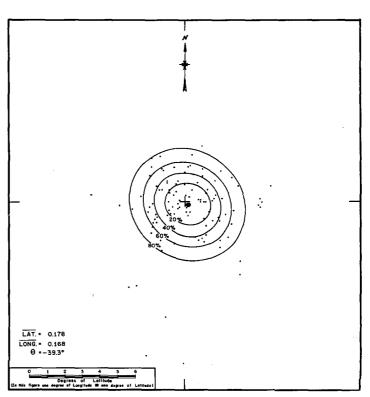


Figure 8.—Probability ellipses for Riehl-Haggard-Sanborn 500-mb. grid method, 24-hr. forecasts, area B (1959-63). For explanation see figure 3.

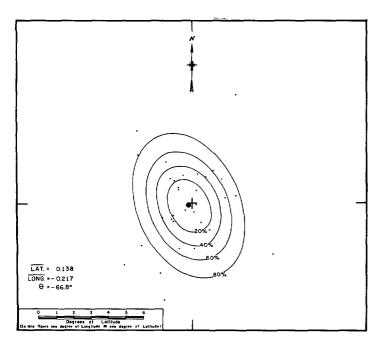


FIGURE 9.—Probability ellipses for Riehl-Haggard-Sanborn 500-mb. grid method, 24-hr. forecasts, area C (1959-63). For explanation see figure 3.

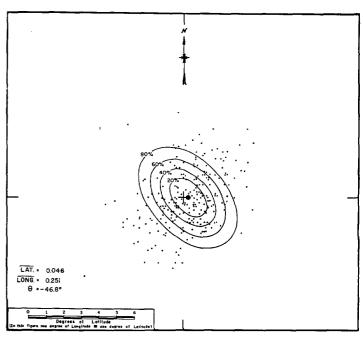


Figure 11.—Probability ellipses for Travelers 1959 (T-59) 24-hr-forecasts, area B (1959-64). For explanation see figure 3.

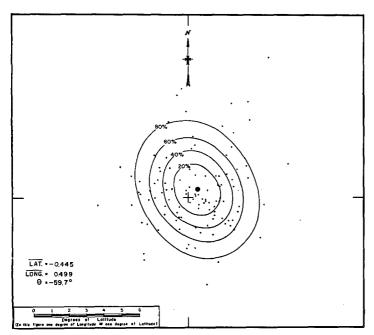


Figure 10.—Probability ellipses for Travelers 1959 (T-59) 24-hr. forecasts, area A (1959-64). For explanation see figure 3.

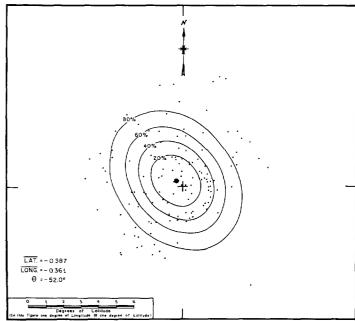
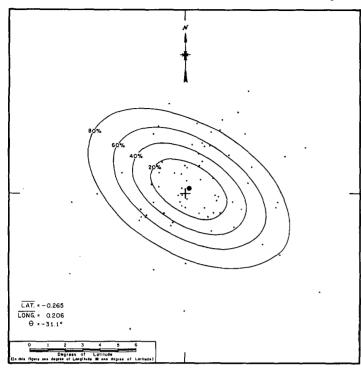
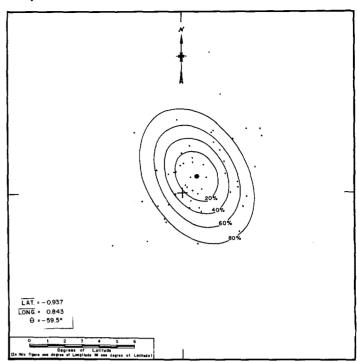


FIGURE 12.—Probability ellipses for Travelers 1959 (T-59) 24-hr. forecasts, area C (1959-64). For explanation see figure 3.





forecasts, area A (1959-64). For explanation see figure 3.

Figure 13.—Probability ellipses for numerical (NWP) 24-hr. Figure 15.—Probability ellipses for numerical (NWP) 24-hr. forecasts, area C (1959-64). For explanation see figure 3.

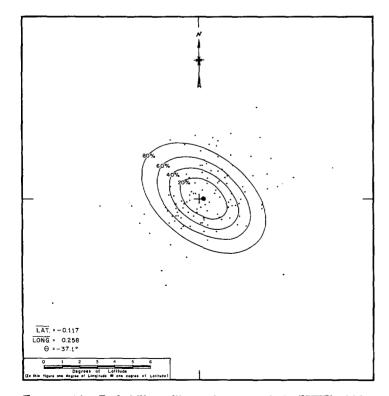


FIGURE 14.—Probability ellipses for numerical (NWP) 24-hr. forecasts, area B (1959-64). For explanation see figure 3.

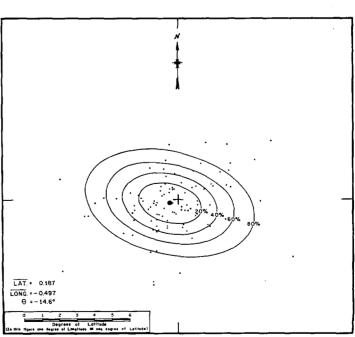


FIGURE 16.—Probability ellipses for Travelers 1960 method (T-60) 24-hr. forecasts, area A (1959-64). For explanation see figure 3.

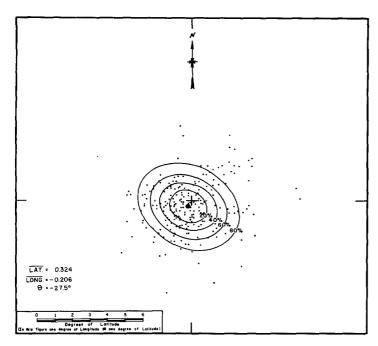


FIGURE 17.—Probability ellipses for Travelers 1960 method (T-60) 24-hr. forecasts, area B (1959-64). For explanation see figure 3.

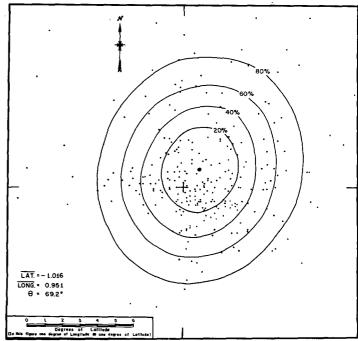


FIGURE 19.—Probability ellipses for persistence forecasts (24-hr.), area A (1959-64). For explanation see figure 3.

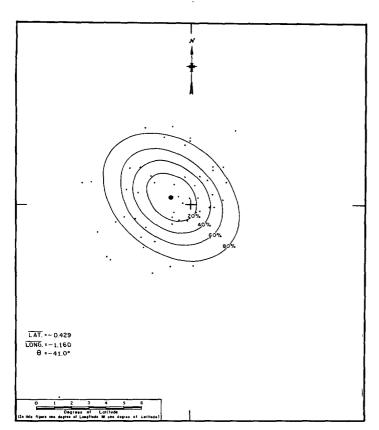


FIGURE 18.—Probability ellipses for Travelers 1960 method (T-60) 24-hr. forecasts, area C (1959-64). For explanation see figure 3.

Forecasts made while storms were in area C by the T-59 and T-60 systems yielded "on the average" forecasts that were too far south and too slow while those using the RHS system were too far north and too slow. Also in the area C, "on the average" forecasts produced by the NWP method were too far south and too fast, those by the M-M method were primarily too slow, those by the PERS method were too fast, and in those by the WB method little bias was shown.

Third, all but three of the techniques (WB-Area A, RHS-Area B, PERS-Area A) for which probability ellipses were determined had shapes that were elliptical. The three which did not, had shapes approximating that of a circle. Contour ellipses having a circular configuration indicate a random distribution of the quantities involved. The more eccentric the ellipses become, the closer the relationship between latitude and longitude errors, and one can see that as the distribution of the vector errors comprising the sample distribution more closely approximates that of a straight line, then the linear correlation coefficient between latitude and longitude errors approaches one.

Fourth, it is apparent, from the section in table 10 containing the percentage of forecasts within probability ellipses, that the probability ellipses for all the figures except figures 3, 16, and 19 represent their respective distributions as valid bivariate normal distributions within

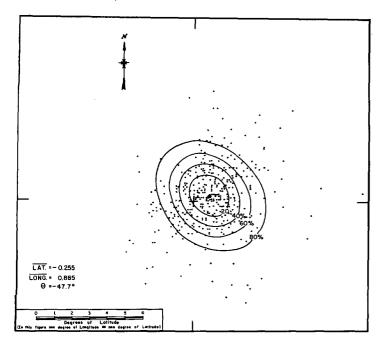


FIGURE 20.—Probability ellipses for persistence forecasts (24-hr.), area B (1959-64). For explanation see figure 3.

the limits of the Kolmogorov-Smirnov test. Strictly speaking, figures 3, 16, and 19 should not appear, as they do not represent close agreement with a bivariate normal distribution. However for the sake of completeness they are presented.

#### **ACKNOWLEDGMENTS**

The author thanks Dr. Banner I. Miller, Dr. R. Cecil Gentry, and Mr. Harry F. Hawkins for their helpful criticisms and comments in the preparation of this paper.

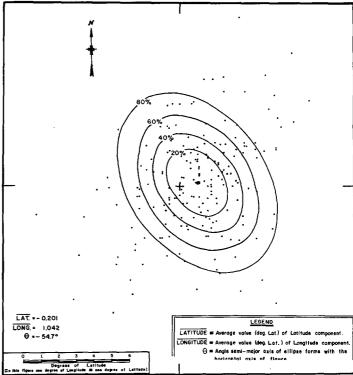
Appreciation is also extended to Mr. Keith W. Veigas of the Travelers Research Center, Inc., Hartford, Conn., for his assistance in certain statistical aspects of the paper.

The author also thanks Messrs. Robert C. Carrodus and Charles H. True for drafting and photographing the figures in this paper.

Final thanks go to Miss Debbie Nejman for typing the manuscript and tables.

## **APPENDIX**

To test a sample of data to see whether it has a bivariate normal distribution, one can utilize the Kolmogorov-Smirnov one-sample test [9] and [6]. This test "... is concerned with the degree of agreement between the distribution of a set of sample values [observed vector errors] and some specified theoretical distribution..." It determines whether the scores in the sample can reasonably be thought to have come from a population having the theoretical distribution. Briefly, the test involves specifying the cumulative frequency distribution which would occur under the theoretical distribution and comparing that with the observed cumulative frequency distri-



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FIGURE 21.—Probability ellipses for persistence forecasts (24-hr.), area C (1959-64). For explanation see figure 3.

bution. The point at which these two distributions, theoretical and observed, show the greatest divergence is determined. Reference to the sampling distribution indicates whether such a large divergence is likely on the basis of chance. That is, the sampling distribution indicates whether a divergence of the observed magnitude would probably occur if the observations were really a random sample from the theoretical distribution.

The Kolmogorov-Smirnov test focuses on the largest of the deviations. The largest value of  $F_0(X) - S_N(X)$  is called the maximum deviation, D:

$$D = maximum |F_0(X) - S_N(X)|$$

where  $F_0$  is a specified cumulative frequency distribution—the theoretical distribution—and  $S_N(X)$  is the observed cumulative frequency distribution of a random sample of N observations.

Values of D at the 5 percent level of significance were determined from the components of the vector errors for each technique and for each area for which forecasts were made. These values of D were then compared with certain critical values which are contained in table E on page 251 of Siegel's [6] book. The results of these tests are presented in table 9 in a different and, perhaps, more interpretative form.

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[Received March 3, 1966; revised April 22, 1966]